

Theory of machinery



Chapter six

Cams

By

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Cams



It is required to in many times to accurately relate the input and output motions through a well defined motion program:

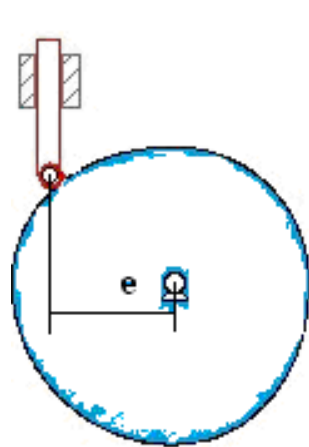
$$y_{out} = F(X_{in}) \text{ ----- function of the input}$$

Cam mechanism provide such a facility between input and output motion by understanding that is the relation between input and output is specified by the shape of cam and other known parameters of the cam mechanism geometry

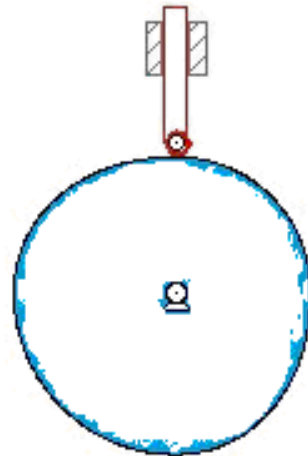
Cams



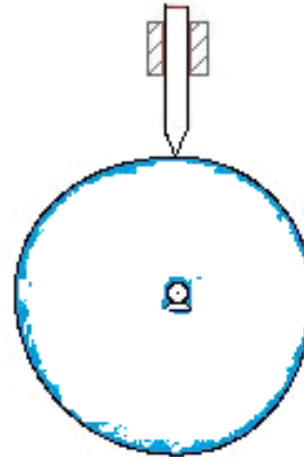
Types of cams



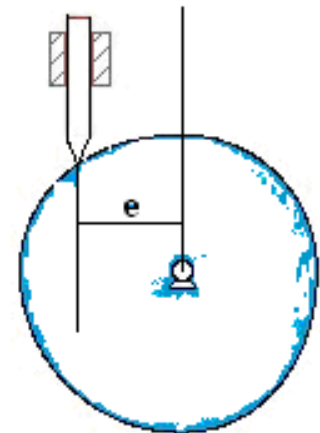
Roller follower
with offset(e)



Roller follower
without offset



edge follower
without offset

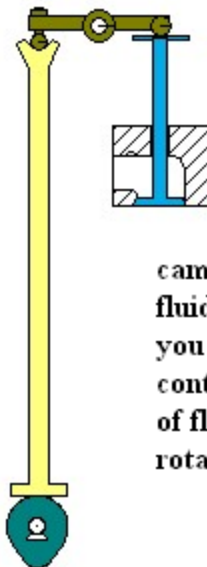
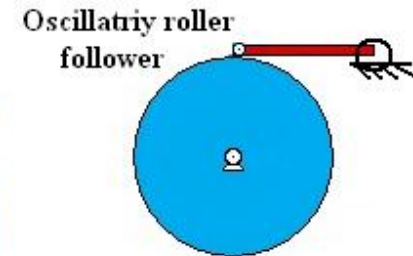
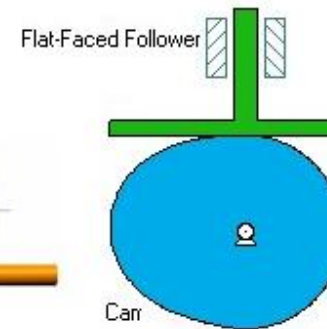
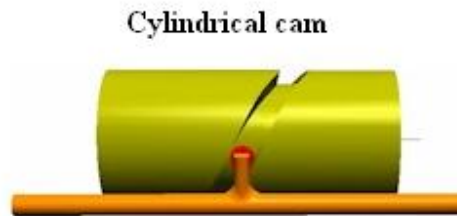
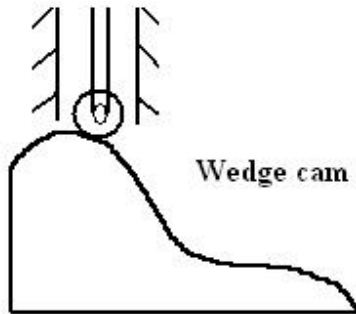


edge follower
with offset(e)

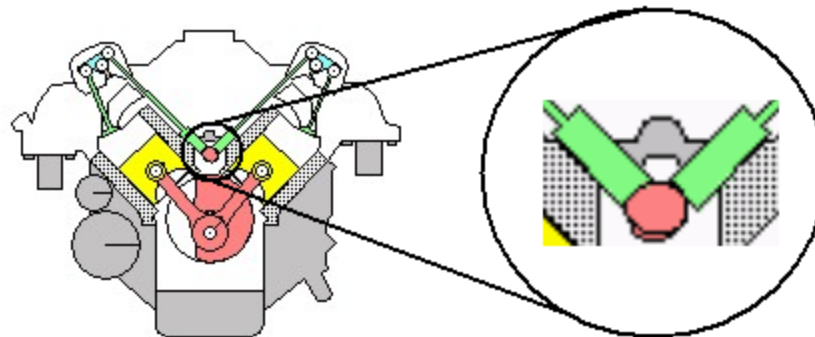
Cams



Types of cams



cam is used in filling fluids in bottles
you can see that cam control the amount of fluid while it rotate

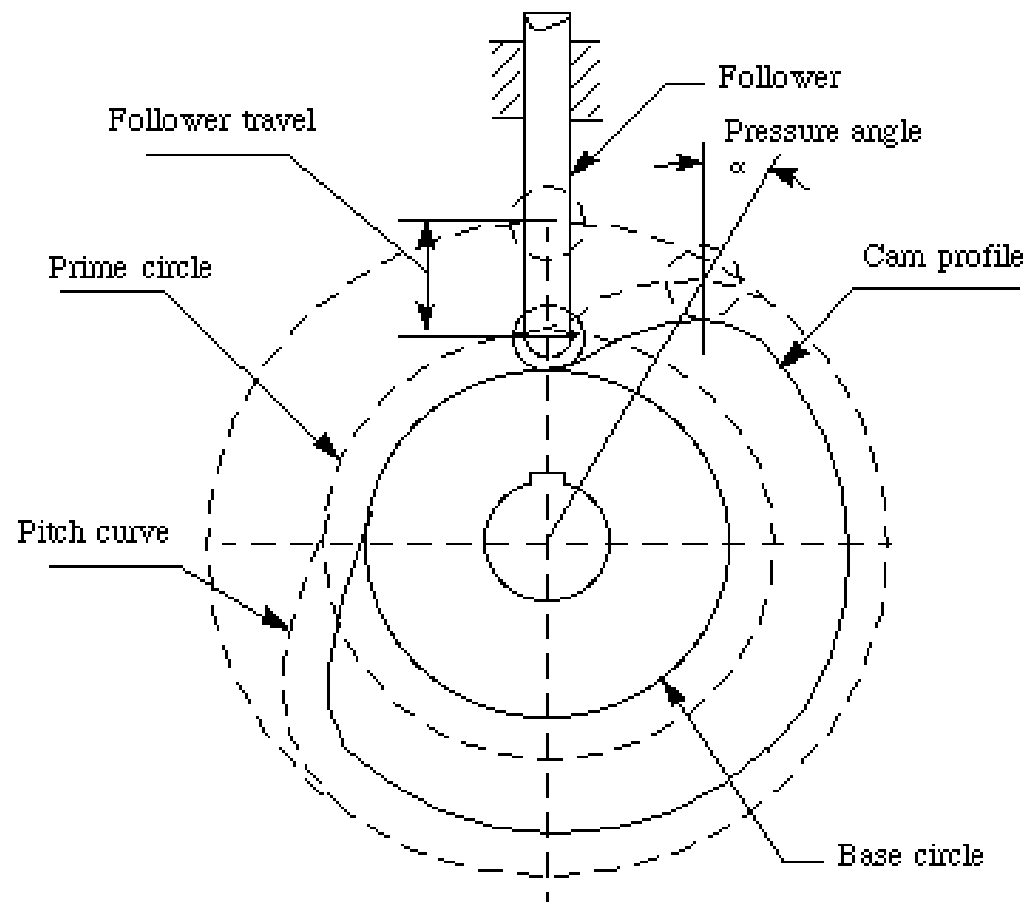


cam used to organize the motion of valves in cars engines

Cams



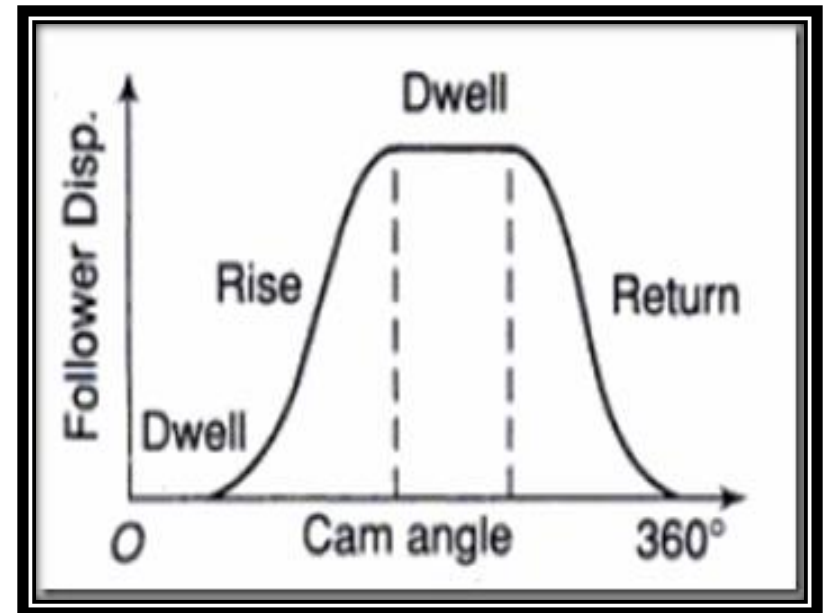
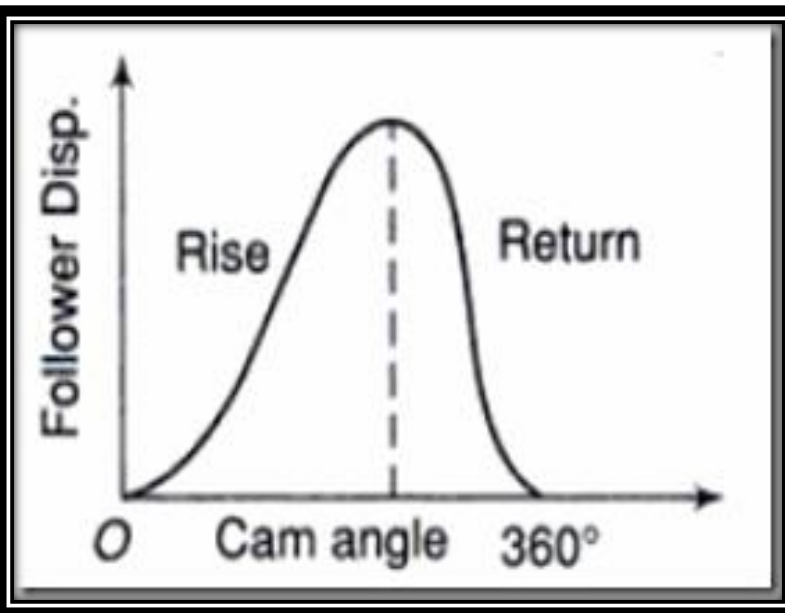
Cam Nomenclature



Cams



Motion segments



Cams



Objectives of Cam

There are two main types of cams according to the task that this cam has to do.

These types are:

1. Give a specific motion to the follower: uniform acceleration and simple harmonic motion (SHM).
2. Cams that have straight lines, circular arcs or other mathematical curves in their profile

For the 1st type, the cam profile is obtained by the geometrical construction

For the 2nd type, the follower displacement is obtained by analytical or graphical methods for any cam angle and the velocity and the acceleration are obtained later by taking the derivatives of the displacement

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Specified motion of the follower

❖ Uniform acceleration and deceleration (parabolic motion)

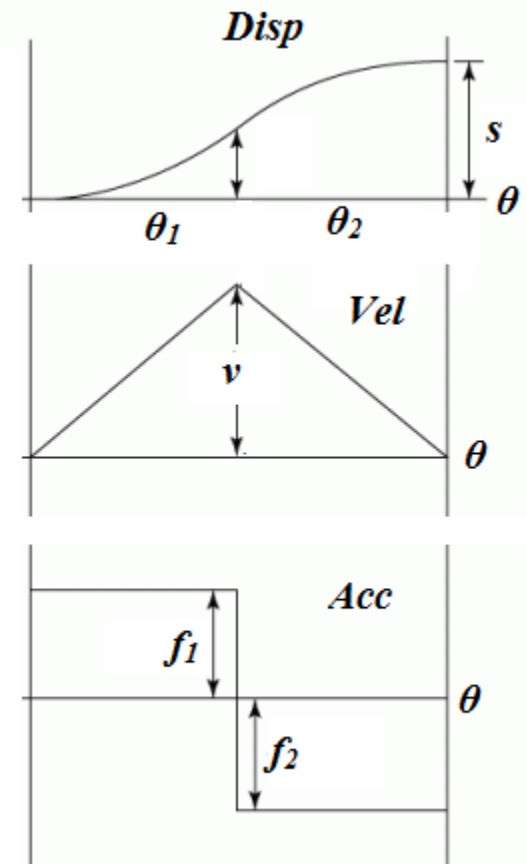
Assume that the follower moves displacement s in time equal t while the cam rotates angle θ and angular velocity ω the following relations are used to find velocity and acceleration

$$t = \frac{\theta}{\omega} \quad v_{mean} = \frac{s}{t} = \frac{\omega s}{\theta} \quad v_{max} = \frac{2s\omega}{\theta}$$

Assume that the acceleration (f_1) occurs in θ_1 and the deceleration (f_2) in θ_2 .

$$f_1 = \frac{v}{t_1} = \frac{2\omega s / \theta}{\theta_1 / \omega} = \frac{2\omega^2 s}{\theta\theta_1}$$

$$f_2 = \frac{v}{t_2} = \frac{2\omega s / \theta}{\theta_2 / \omega} = \frac{2\omega^2 s}{\theta\theta_2}$$



❖ **Parabolic motion** is a one example of constant acceleration motion cam

Cams



Specified motion of the follower

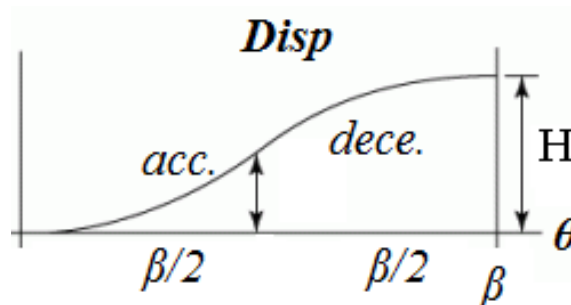
❖ Uniform acceleration and deceleration (parabolic motion)

The following equations represent the follower motion program:

$$S = 2H \left(\frac{\theta}{\beta} \right)^2; \quad 0 < \theta < \beta/2 \quad S = H \left(1 - 2 \left(1 - \frac{\theta}{\beta} \right)^2 \right); \quad \beta/2 < \theta < \beta$$

$$\dot{S} = 4H\omega \left(\frac{\theta}{\beta^2} \right); \quad 0 < \theta < \beta/2 \quad \dot{S} = 4H \frac{\omega}{\beta} \left(1 - \frac{\theta}{\beta} \right); \quad \beta/2 < \theta < \beta$$

$$\ddot{S} = 4H \left(\frac{\omega}{\beta} \right)^2; \quad 0 < \theta < \beta/2 \quad \ddot{S} = -4H \left(\frac{\omega}{\beta} \right)^2; \quad \beta/2 < \theta < \beta$$



Cams



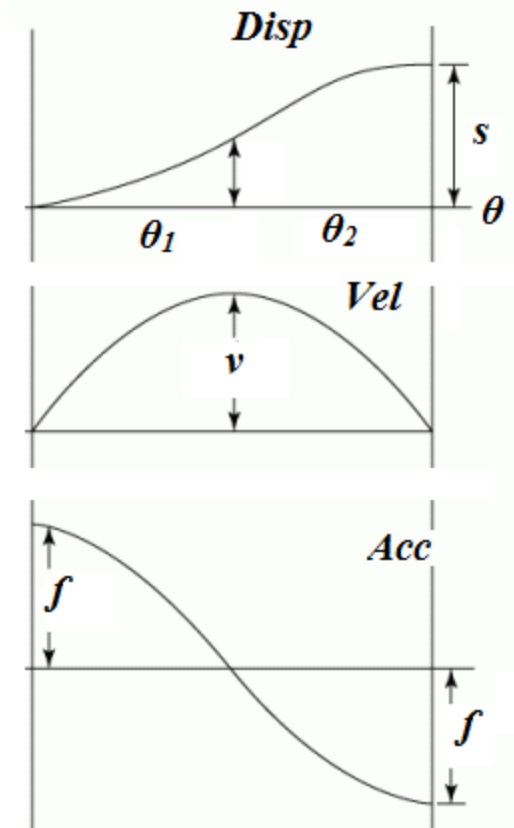
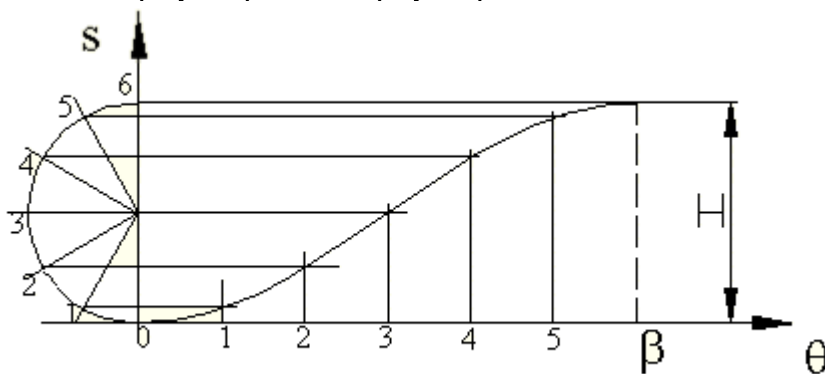
Specified motion of the follower

❖ Simple harmonic motion

The curve is the projection of a circle about the cam rotation axis. The following relations are used to find velocity and acceleration

$$s(\theta) = \frac{H}{2} \left(1 - \cos \left(\frac{\pi \theta}{\beta} \right) \right) \quad \dot{s}(\theta) = \frac{H}{2} \left(\frac{\pi \omega}{\beta} \right) \sin \left(\frac{\pi \theta}{\beta} \right)$$

$$\ddot{s}(\theta) = \frac{H}{2} \left(\frac{\pi \omega}{\beta} \right)^2 \cos \left(\frac{\pi \theta}{\beta} \right)$$



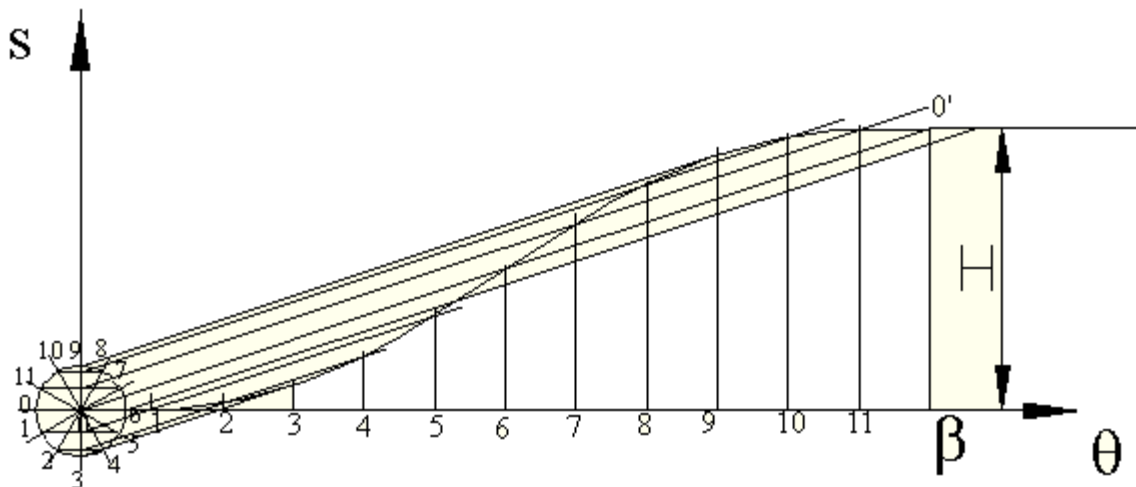
Cams



Specified motion of the follower

❖Cyclodial motion

The circumference of the circle is equal to the total rise; or the diameter is H/p . The circumference is divided into a number of equal parts corresponding to the divisions along the horizontal axis. The points around the circle are first projected to the vertical centerline of the circle and then parallel to OO' to the corresponding vertical line on the diagram.



Cams

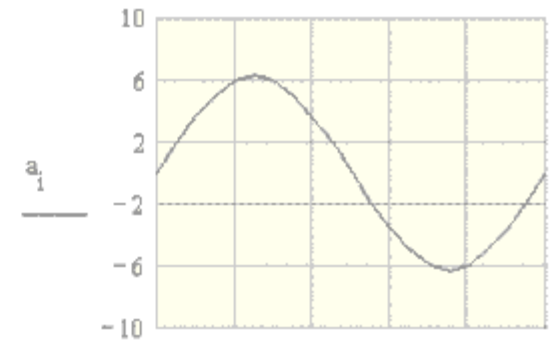
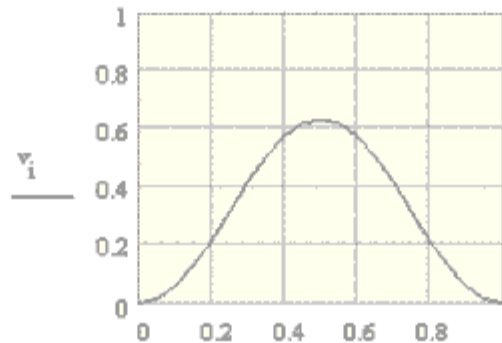
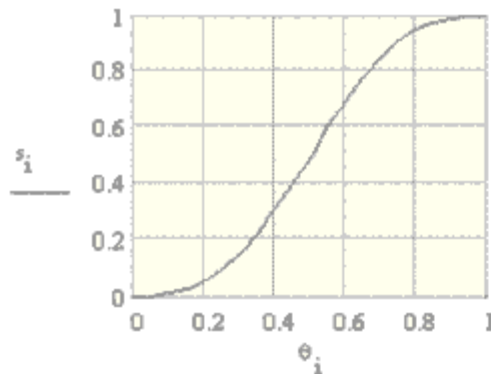


Specified motion of the follower

❖Cyclodial motion

The relations and graphs for the cam are

$$s(\theta) = \frac{h}{\pi} \left(\frac{\pi\theta}{\beta} - \frac{1}{2} \sin \left(\frac{2\pi\theta}{\beta} \right) \right) \quad \dot{s}(\theta) = \frac{h}{\pi} \left(\frac{\omega}{\beta} \right) \left(1 - \cos \left(\frac{2\pi\theta}{\beta} \right) \right) \quad \ddot{s}(\theta) = 2h\pi \left(\frac{\omega}{\beta} \right)^2 \sin \left(\frac{2\pi\theta}{\beta} \right)$$



Cams



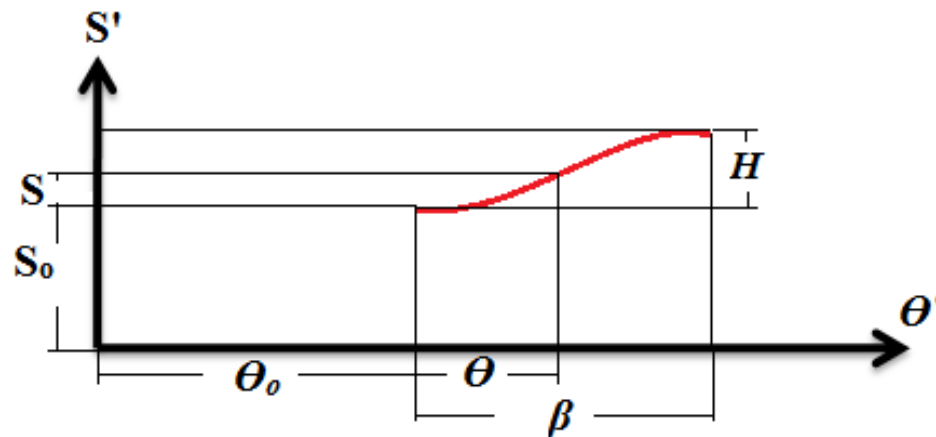
Specified motion of the follower

❖ Application of motion laws

the three types of specified motions (parabolic, SHM and cycloidal) are designed to find the follower displacement depending on one condition:

The follower displacement equal zero when the cam angle is also zero

however, if the segment doesn't satisfy this condition, a shifting procedure must be applied. To illustrate this procedure, let us assume there is a rise segment starts from S_0 and Θ_0 as shown in the figure.



Cams



Specified motion of the follower

❖ Application of motion laws

According to this shifting procedure :

$$S' = S_o \pm S(\theta); + \text{ if rise and } - \text{ if return}$$

$$\theta' = \theta_o + \theta$$

where: $0 < \theta < \beta$ and $\theta = \theta' - \theta_o$.

$$r_c = r_b + s.$$

Where:

r_b = basic circle radius

r_c = cam profile radius

Cams



Example

Draw the cam profile needed to achieve:

- ☐ Follower is edge
- ☐ base radius = 5 cm
- ☐ $0 \rightarrow 90^\circ$: SHM rise to 3cm
- ☐ $90^\circ \rightarrow 180^\circ$: Dwell
- ☐ $180^\circ \rightarrow 270^\circ$: SHM return to 0
- ☐ $270^\circ \rightarrow 360^\circ$: Dwell

Cams



Example

Solution:

□ $0 \rightarrow 90^\circ$: SHM rise to 3cm $s(\theta) = \frac{H}{2} \left(1 - \cos \left(\frac{\pi\theta}{\beta} \right) \right) = \frac{3}{2} [1 - \cos(2\theta)]$

□ $90^\circ \rightarrow 180^\circ$: Dwell $\rightarrow S = 3\text{cm}$

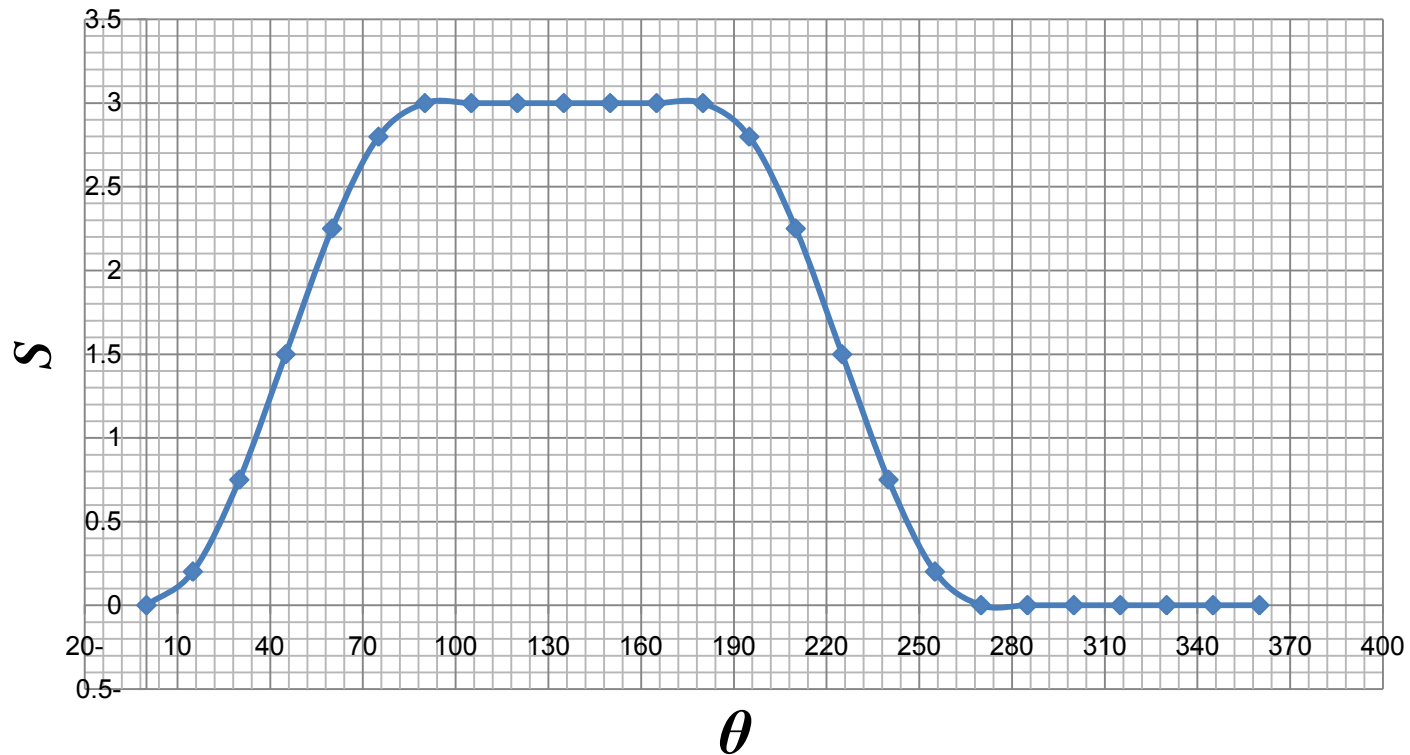
□ $180^\circ \rightarrow 270^\circ$: SHM return to 0 $s(\theta) = \cancel{3} - \left\{ \frac{3}{2} [1 - \cos(2\theta)] \right\}$

□ $270^\circ \rightarrow 360^\circ$: Dwell $\rightarrow S = 0\text{ mm}$

Cams



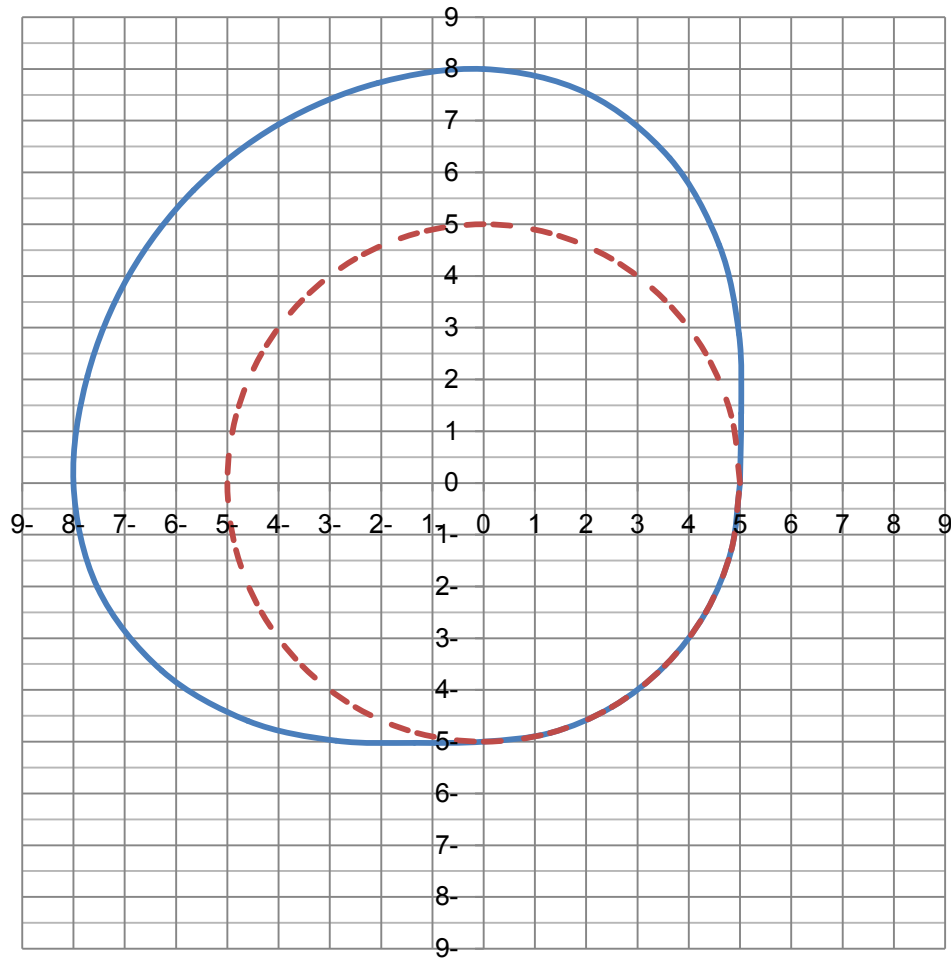
Example



Cams



Example

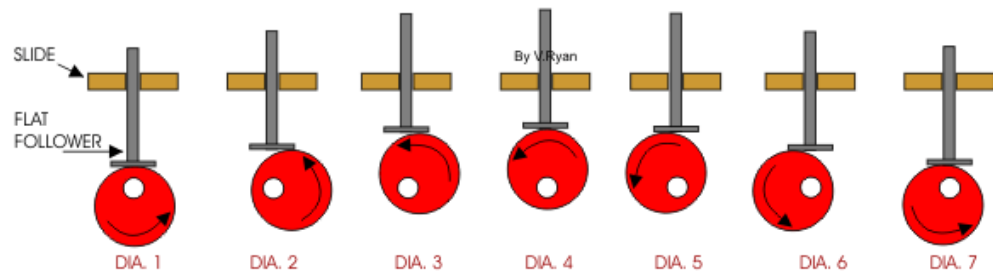
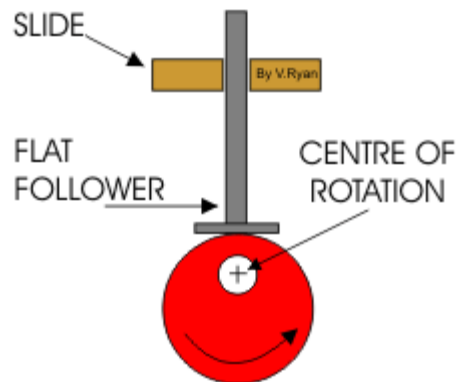


Cams



Eccentric circular cam

- ❑ Eccentric cam is a cam has the axis of rotation **not** in the center
- ❑ This type of cams depend on the eccentricity to create the follower motion
- ❑ When the cam rotate, the distance with respect to the follower (h) changes depending on the value of the eccentricity (e)



Cams



Eccentric circular cam

Eccentric cam is a cam has the axis of rotation **not** in the center

$$h = e\{1 - \cos(\theta)\}$$

$$v = \frac{dh}{dt} = \frac{dh}{d\theta} \frac{d\theta}{dt} = \frac{dh}{d\theta} \omega$$

$$\Rightarrow v = \omega e \sin(\theta)$$

$$a = \frac{dv}{dt} = \frac{dv}{d\theta} \frac{d\theta}{dt}$$

$$\Rightarrow a = \omega^2 e \cos(\theta)$$

